## חAmIBIA UחIVERSITY

OF SCIEПCE AПD TECHחOLOGY

## FACULTY OF MANAGEMENT SCIENCES

## DEPARTMENT OF MARKETING AND LOGISTICS

| QUALIFICATION: BACHELOR OF LOGIST HONOURS | AND SUPPLY CHAIN MANAGEMENT |
| :---: | :---: |
| QUALIFICATION CODE: 08HLSCH | LEVEL: 8 |
| COURSE: FINANCIAL TECHNIQUES FOR LOGISTICS MANAGEMENT OPERATIONS | COURSE CODE: FTL 821S |
| SESSION: NOVEMBER 2019 | PAPER: THEORY AND PRACTICAL |
| DURATION: 3 HOURS | MARKS: 100 |


| FIRST OPPORTUNITY EXAMINATION QUESTION PAPER |  |
| :--- | :--- |
| EXAMINER | Mr. T. Nakweenda (UNAM) |
| MODERATOR: | Mr. Johannes Ndjuluwa (UNAM) |

## INSTRUCTIONS

1. Answer all questions.
2. Number your answers accordingly.
3. The use of PV and FV tables attached as appendix is permissible.
4. Round your final answers to two decimal places wherever applicable.

THIS QUESTION PAPER CONSISTS OF 6 PAGES (including this front page)

## Question 1 (10 Marks, 18 Minutes)

Suppose you have been appointed as an intern responsible for financial matters at Logistics Management Ltd ("LM"). LM's Managing Director has been reliably informed that you are an expert when it comes to financial matters. You are required to assist him understand each of the following questions.

| REQUIRED: Be concise as much as possible. |  | MARKS |
| :---: | :--- | :---: |
| 1.1. | In your own words, define the term finance (a) at a personal level, and (b) <br> in a business context. | 3 |
| 1.2. | Describe the goal of the firm clearly explaining why maximizing the value <br> of the firm is an appropriate goal for a business. | 3 |
| 1.3. | Identify two common legal forms of business organizations and clearly <br> distinguish how such identified legal forms of business organizations are <br> different from one another in terms of their respective liability. | 4 |
| TOTAL MARKS | $\mathbf{1 0}$ |  |

## Question 2 ( 30 Marks, 54 Minutes)

This question is divided into two parts, namely: 2.1 and 2.2, which are independent of each other. Each part should, therefore, be answered in the context in which it has been asked. Any assumptions made should be clearly indicated as such.

## 2.1. (18 Marks, 32 Minutes)

Analysis of Annual Financial Statements ("AFS") is one of the critical tasks performed by financial analysts. Companies A and B ("Co. A and $\mathrm{Co} . \mathrm{B}$ ") are competitors in a manufacturing industry. The two companies have been rivals almost for five years now. Mr. Simon is a potential investor who is uncertain as into which of the two companies he should invest. You have been provided with the following information in respect of the two companies:

$\left.$|  | Note | N\$ | N\$. A |
| :--- | :---: | ---: | ---: | | Co. B |
| ---: | \right\rvert\,

1. $60 \%$ of Co. A sales is on credit, while Co. B has a policy of $50 \%$ credit and $50 \%$ cash.
2. $10 \%$ of Co. A total current assets represent inventory. This is one percent more compared to Co. B. Accordingly, the two companies' Accounts Receivable amount to $20 \%$ and $18 \%$ of their total current assets, respectively.
3. Assume a 360 days calendar year.

| REQUIRED: Clearly show all your workings wherever applicable. | MARKS |  |
| :--- | :--- | :---: |
| 2.1 .1. | For each company, calculate the following financial ratios: <br> a. Current ratio <br> b. Quick ratio <br> c. Gross margin ratio <br> d. Average Collection Period ("ACP") | 10 |
| 2.1 .2. | Critically comment on each of the ratio calculated in 2.1.1. In your <br> discussion, clearly indicate to which ratio category such a ratio belongs. | 7 |
| 2.1 .3. | On the basis of Quick ratio and ACP, which one of the two rival <br> companies would you recommend to Mr. Simon? Briefly explain your <br> answer. | 1 |
| TOTAL MARKS FOR 2.1. | $\mathbf{1 8}$ |  |

## 2.2. (12 Marks, 22 Minutes)

Lack of housing is one of the daunting tasks among professionals. Though the current economic situation seems to have led to a drop in property prices, the majority of professionals are still finding it hard to buy a property. Ms. Kadhepa is one of such professionals. She has been renting almost close to twenty years now. Being in her late 50s, she has recently applied for a mortgage bond at FNB Home Loans, and she was provided with the following information:

- Qualified amount
- Repayment period
- Deposit

N\$ 1500000 @ 10\% p.a.
10 years
0\%

| REQUIRED: Clearly show all your workings. | MARKS |  |
| :---: | :--- | :---: |
| 2.2.1. | Calculate the yearly instalment that to be paid by Ms. Kadhepa. | 1.5 |
| 2.2.2. | Prepare an Amortization table clearly showing the: instalment; capital; <br> interest and end balance. | 9.5 |


| 2.2.3. | What constitutes the instalment amount? | 1 |
| :--- | :--- | :---: |
| TOTAL MARKS FOR 2.2. | $\mathbf{1 2}$ |  |
| TOTAL MARKS FOR QUESTION 2 | $\mathbf{3 0}$ |  |

## Question 3 (15 Marks, 27 Minutes)

Namib Breweries Ltd ("NB") has 100, $8 \%$ bonds in issue with a nominal value of $\mathrm{N} \$ 1000$ each. These bonds will be redeemed in four years' time at their nominal value. Similar bonds currently trade at $12 \%$ per annum in the general market. As a current practice, coupons are paid annually. Given your expertise in financial techniques, suppose you have been hired by NB to serve as their market consultant. The Managing Director ("MD") of NB has requested you to assist with the following calculations:

| REQUIRED: |  | MARKS |
| :---: | :--- | :---: |
| 3.1. | Compute the present value of NB's bond based on the current practice. | 3.5 |
| 3.2. | Suppose NB's MD is of the opinion that it would be cheaper to pay <br> coupons on a quarterly basis. Do you agree with the MD? Show all your <br> workings. | 6.5 |
| 3.3. | Identify four features associated with a bond. | 5 |
| TOTAL MARKS FOR QUESTION 3 | $\mathbf{1 5}$ |  |

## Question 4 (15 Marks, 27 Minutes)

Making an informed investment decision is one of the essential tasks more especially in the current economy. Investors are inclined to first assess every risk which might be associated with their respective investment. Assume that you are a financial analyst at one of the local equity brokers. Suppose you have predicted the following returns for shares $A$ and $B$ in three possible states of the economy:

|  |  | Share type |  |
| :--- | :---: | :---: | :---: |
| State of economy | Probability | A | B |
| Boom | 0.50 | 0.15 | 0.20 |
| Normal | 0.30 | 0.10 | 0.15 |
| Recession | $?$ | 0.05 | 0.02 |

A risk averse potential investor would like to invest in either of the two shares. Generally, a typical risk averse investor would monitor closely the risk associated with his investment. In the event where a mutually investment is yielding the same returns, a standard deviation is used as
a basis of such a decision. Assume that the two shares are mutually exclusive, and they belong to an industrial sector.

| REQUIRED: Clearly show all your workings. |  | MARKS |
| :---: | :--- | :---: |
| 4.1. | Compute the expected returns for each share. | 4 |
| 4.2. | Compute the standard deviation associated with each share. | 5 |
| 4.3. | On the basis of standard deviation, which one of the two shares would you <br> recommend to the prospective risk averse investor, and why? | 3 |
| 4.4. | Suppose the risk averse investor decides to invest 60\% of his funds in your <br> recommended share as per 4.1.3, and 40\% in a 'different sector'. What do <br> you think will happen to the standard deviation of such a portfolio? | 3 |
| TOTAL MARKS FOR QUESTION 4 | $\mathbf{1 5}$ |  |

## Question 5 ( 30 Marks, 54 Minutes)

This question is divided into two parts, namely: 5.1 and 5.2. The two parts are independent of each other. Each part should, therefore, be answered in the context in which questions thereof have been asked.

## 5.1. (18 Marks, 32 Minutes)

According to the Namibia Statistics Agency (NSA) Labour Force Survey of 2018, the country has witnessed enormous retrenchments. The most affected sectors are construction, fisheries and agriculture. This has contributed to the already high rate of unemployment in the country. As a remedial measure, graduates are encouraged to venture into entrepreneurship.

As a Logistics and Supply Chain Management expertise, suppose you have secured funding of N\$ 100, 000 from the Development Bank of Namibia. This was after you provided them with a detailed business plan, which as a result; convinced them about your proposed business acumen.

You intend to invest part of this funding either in a Shuttle business or Car wash business. According to market research, the two businesses have similar business risk. Suppose you decide to invest $80 \%$ of your funding in either. Shuttle business ("SB") would result in annual cash inflows of N\$ 25000 in years 1 through year 5 . On the other hand, the Car was business ("CwB") would result in annual cash inflows of $\mathrm{N} \$ 23000$ in years 1 through year 5. All the two prospective businesses have equal economic useful lives of five years. All the above mentioned
cash inflows are assumed to be adjusted for depreciation. Assume a cost of capital of $12 \%$ per annum.

| REQUIRED: Clearly show all your workings. | MARKS |  |
| :--- | :--- | :---: |
| 5.1.1. | Apart from the secured funds from DBN, under each proposed project, <br> identify two factors that you should consider before attempting to venture <br> into it. Be realistic as much as possible. | 6 |
| 5.1.2. | Which one of the two proposed projects should be chosen on the basis of <br> the following techniques: <br> a. Net Present Value (NPV), <br> b. Pay Back Period (PBP), your answer should be expressed in years, <br> months and days. | 12 |
| c. Based on your answers in (a) and (b), are there any conflicting <br> recommendations. If so, which of the two techniques would you opt <br> for and why? | $\mathbf{1 8}$ |  |
| TOTAL MARKS FOR 5.1 |  |  |

## 5.2. (12 Marks, 22 Minutes)

Proper inventory management is key to every business. Thus, if poorly managed, a business may encounter serious cash flow problems. Suppose you have been appointed as Procurement Manager at Community Bakery Cc ("CB"). CB bakes bread daily for a school feeding project. It purchases flour in 50 kilograms bags at $\mathrm{N} \$ 250$ per bag and uses 400 of these bags every month. The cost of placing an order per bag is $\mathrm{N} \$ 5.50$, and the administrative cost per bag is $\mathrm{N} \$ 4.50$. Storage cost is $\mathrm{N} \$ 9.60$ per bag per annum. Assume a 360 days calendar year.

| REQUIRED: Compute the following: | MARKS |  |
| :--- | :--- | :---: |
| 5.2.1. | Economic Order Quantity (EOQ). | 4 |
| 5.2 .2. | Number of orders that should be placed per annum. | 2 |
| 5.2 .3. | Total; ordering and holding cost per annum. | 3 |
| 5.2 .4. | Total annual inventory cost based on the given information. | 3 |
| TOTAL MARKS FOR 5.2. | 12 |  |
| TOTAL MARKS FOR QUESTION 5 | 30 |  |


| Futu | valu | inter | t | tor of | 1 | fo | per | , F | (i,n) | \$1* | i ) ${ }^{\text {n }}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Period | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |
| 1 | 1.010 | 1.020 | 1.030 | 1.040 | 1.050 | 1.060 | 1.070 | 1.080 | 1.090 | 1.100 | 1.110 | 1.120 | 1.130 | 1.140 | 1.150 | 1.160 | 1.170 | 1.180 | 1.190 | 1.200 |
| 2 | 1.020 | 1.040 | 1.061 | 1.082 | 1.103 | 1.124 | 1.145 | 1.166 | 1.188 | 1.210 | 1.232 | 1.254 | 1.277 | 1.300 | 1.323 | 1.346 | 1.369 | 1.392 | 1.416 | 1.440 |
| 3 | 1.030 | 1.061 | 1.093 | 1.125 | 1.158 | 1.191 | 1.225 | 1.260 | 1.295 | 1.331 | 1.368 | 1.405 | 1.443 | 1.482 | 1.521 | 1.561 | 1.602 | 1.643 | 1.685 | 1.728 |
| 4 | 1.041 | 1.082 | 1.126 | 1.170 | 1.216 | 1.262 | 1.311 | 1.360 | 1.412 | 1.464 | 1.518 | 1.574 | 1.630 | 1.689 | 1.749 | 1.811 | 1.874 | 1.939 | 2.005 | 2.074 |
| 5 | 1.051 | 1.104 | 1.159 | 1.217 | 1.276 | 1.338 | 1.403 | 1.469 | 1.539 | 1.611 | 1.685 | 1.762 | 1.842 | 1.925 | 2.011 | 2.100 | 2.192 | 2.288 | 2.386 | 2.488 |
| 6 | 1.062 | 1.126 | 1.194 | 1.265 | 1.340 | 1.419 | 1.501 | 1.587 | 1.677 | 1.772 | 1.870 | 1.974 | 2.082 | 2.195 | 2.313 | 2.436 | 2.565 | 2.700 | 2.840 | 2.986 |
| 7 | 1.072 | 1.149 | 1.230 | 1.316 | 1.407 | 1.504 | 1.606 | 1.714 | 1.828 | . 949 | 2.076 | 2.211 | 2.353 | 2.502 | 2.660 | 2.826 | 3.001 | 3.185 | 3.379 | 3.583 |
| 8 | 1.083 | 1.172 | 1.267 | 1.369 | 1.477 | 1.594 | 1.718 | 1.851 | 1.993 | 2.144 | 2.305 | 2.476 | 2.658 | 2.853 | 3.059 | 3.278 | 3.511 | 3.759 | 4.021 | 4.300 |
| 9 | 1.094 | 1.195 | 1.305 | 1.423 | 1.551 | 1.689 | 1.838 | 1.999 | 2.172 | 2.358 | 2.558 | 2.773 | 3.004 | 3.252 | 3.518 | 3.803 | 4.108 | 4.435 | 4.785 | 5.160 |
| 10 | 1.105 | 1.219 | 1.344 | 1.480 | 1.629 | 1.791 | 1.967 | 2.159 | 2.367 | 2.594 | 2.839 | 3.106 | 3.395 | 3.707 | 4.046 | 4.411 | 4.807 | 5.234 | 5.695 | 6.192 |
| 11 | 1.116 | 1.243 | 1.384 | 1.539 | 1.710 | 1.898 | 2.105 | 2.332 | 2.580 | 2.853 | 3.152 | 3.479 | 3.836 | 4.226 | 4.652 | 5.117 | 5.624 | 6.176 | 6.777 | 7.430 |
| 12 | 1.127 | 1.268 | 1.426 | 1.601 | 1.796 | 2.012 | 2.252 | 2.518 | 2.813 | 3.138 | 3.498 | 3.896 | 4.335 | 4.818 | 5.350 | 5.936 | 6.580 | 7.288 | 8.064 | 8.916 |
| 3 | 1.138 | 1.294 | 1.469 | 1.665 | 1.886 | 2.133 | 2.410 | 2.720 | 3.066 | 3.452 | 3.883 | 4.363 | 4.898 | 5.492 | 6.153 | 6.886 | 7.699 | 8.599 | 9.596 | 10.699 |
| 14 | 1.149 | 1.319 | 1.513 | 1.732 | 1.980 | 2.261 | 2.579 | 2.937 | 3.342 | 3.797 | 4.310 | 4.887 | 5.535 | 6.261 | 7.076 | 7.988 | 9.007 | 10.147 | 11.420 | 12.839 |
| 15 | 1.161 | 1.346 | 1.558 | 1.801 | 2.079 | 2.397 | 2.759 | 3.172 | 3.642 | 4.177 | 4.785 | 5.474 | 6.254 | 7.138 | 8.137 | 9.266 | 10.539 | 11.974 | 13.590 | 15.407 |
| 16 | 1.173 | 1.373 | 1.605 | 1.873 | 2.183 | 2.540 | 2.952 | 3.426 | 3.970 | 4.595 | 5.311 | 6.130 | 7.067 | 8.137 | 9.358 | 10.748 | 12.330 | 14.129 | 16.172 | 18.488 |
| 17 | 1.184 | 1.400 | 1.653 | 1.948 | 2.292 | 2.693 | 3.159 | 3.700 | 4.328 | 5.054 | 5.895 | 6.866 | 7.986 | 9.276 | 10.761 | 12.468 | 14.426 | 16.672 | 19.244 | 22.186 |
| 18 | 1.196 | 1.428 | 1.702 | 2.026 | 2.407 | 2.854 | 3.380 | 3.996 | 4.717 | 5.560 | 6.544 | 7.690 | 9.024 | 10.575 | 12.375 | 14.463 | 16.879 | 19.673 | 22.901 | 26.623 |
| 19 | 1.208 | 1.457 | 1.754 | 2.107 | 2.527 | 3.026 | 3.617 | 4.316 | 5.142 | 6.116 | 7.263 | 8.613 | 10.197 | 12.056 | 14.232 | 16.777 | 19.748 | 23.214 | 27.252 | 31.948 |
| 20 | 1.220 | 1.486 | 1.806 | 2.191 | 2.653 | 3.207 | 3.870 | 4.661 | 5.604 | 6.727 | 8.062 | 9.646 | 11.523 | 13.743 | 16.367 | 19.461 | 23.106 | 27.393 | 32.429 | 38.338 |
| 25 | 1.282 | 1.641 | 2.094 | 2.666 | 3.386 | 4.292 | 5.427 | 6.848 | 8.623 | 10.835 | 13.585 | 17.000 | 21.231 | 26.462 | 32.919 | 40.874 | 50.658 | 62.669 | 77.388 | 95.396 |
| 30 | 1.348 | 1.811 | 2.427 | 3.243 | 4.322 | 5.743 | 7.612 | 10.063 | 13.268 | 17.449 | 22.892 | 29.960 | 39.116 | 50.950 | 66.212 | 85.850 | 111.065 | 143.371 | 184.675 | 237.376 |
| 35 | 1.417 | 2.000 | 2.814 | 3.946 | 5.516 | 7.686 | 10.677 | 14.785 | 20.414 | 28.102 | 38.575 | 52.800 | 72.069 | 98.100 | 133.176 | 180.314 | 243.503 | 327.997 | 440.701 | 590.668 |
| 40 | 1.489 | 2.208 | 3.262 | 4.801 | 7.040 | 10.286 | 14.974 | 21.725 | 31.409 | 45.259 | 65.001 | 93.051 | 132.782 | 188.884 | 267.864 | 378.721 | 533.869 | 750.378 | 1,051.668 | 1,469.772 |
| 50 | 1.645 | 2.692 | 4.384 | 7.107 | 11.467 | 18.420 | 29.457 | 46.902 | 74.358 | 117.391 | 184.565 | 289.002 | 450.736 | 700.233 | 1,083.657 | 1,670.704 | 2,566.215 | 3,927.357 | 5,988.914 | 9,100.438 |


| Present value interest factor of \$1 at $\mathrm{i} \%$ for n periods, $\operatorname{PVIF}(\mathrm{i}, \mathrm{n})=(1 /(1+\mathrm{i}))^{\wedge}(\mathrm{n})$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{\|l\|} \hline \text { Prese } \\ \hline \text { Period } \\ \hline \end{array}$ | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% 10\% |  | 11\% | 12\% | 13\% | 14\% | 15\% | 6\% | 17\% | 8\% | 19\% | 20\% |
|  | 0.990 | 0.98 | 0.971 | . 962 | 0.952 | 0.943 | 935 | 0.926 | 0.917 | 0.909 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.8 | 0.840 | 0.833 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.9 | 0.890 | 873 | 0.857 | 0.842 | 0.826 | 0.812 | 0.79 | 0.78 | 0.76 | 0.756 | 0.7 | 0.731 | 0.71 | 0.7 | 0.69 |
| 3 | 0.97 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.77 | 0.751 | 0.73 | 0.7 | 0.6 | 0.67 | 0.658 | 0.6 | 0.624 | 0.6 | 0.5 | 0.579 |
| 4 | 0.961 | 0.924 |  | 855 | 0.823 | - 192 | , 76 | . 73 | 0.708 | 0.683 | 0.65 | 0.63 | 0.6 | 0.59 | 0.572 | 0.5 | 0.5 | 0.5 | 0.49 | 0.482 |
| 5 | 0.951 | 0.906 | . 63 | 822 | 0.784 | 0.747 | 713 | . 68 | 0.650 | 0.621 | 0.59 | 0.56 | 0.5 | 0.51 | 0.49 | 0.4 | 0.456 | 0.4 | 0.419 | 0.402 |
| 6 | 0.9 | 0.888 | 0.837 | 790 | . 74 | 0.705 | 0.666 | 0.630 | 0.596 | 564 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 |
| 7 | 0.933 | 0.871 | 0.813 | 760 | 711 | 0.665 | . 62 | 0.58 | 0.54 | 0.513 | 0.48 | 0.452 | 0.42 | 0.400 | 0.376 | 0.35 | 0.333 | 0.31 | 0.2 | 0.279 |
| 8 | 0.923 | 0.853 | 0.7 | 731 | . 67 | 0.627 | 0.58 | 0.540 | . 502 | 0.467 | 0.43 | 0.40 | 0.37 | 0.35 | 0.32 | 0.30 | 0.2 | 0.266 | 0.249 | 0.233 |
| 9 | 0.914 | 0.837 | 0 | 703 | 645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 0.391 | 0.361 | 0.33 | 0.30 | 0.284 | 0.26 | 0.243 | 0.22 | 0.2 | 0.19 |
| 10 | 0.905 | 820 | 0.744 | 676 | 614 | 0.558 | 508 | 463 | 0.422 | 386 | 0.35 | 0.322 | 0.29 | 0.2 | 0.2 | 0.22 | 0.208 | 0.19 | 0.1 | 0.162 |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 475 | 0.429 | 0.388 | 0.350 | 0.31 | 0.287 | 0.26 | 0.23 | 0.215 | 0.19 | 0.178 | 0.16 | 0.1 | 0.135 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 444 | 0.397 | 0.356 | 0.319 | 0.28 | 0.25 | 0.23 | 0.20 | 0.187 | 0.1 | 0.15 | 0.13 | 0.12 | 0.112 |
| 13 | 0.879 | 73 | 81 | 0.601 | 530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 0.25 | 0.2 | 0.20 | 0.1 | 0.163 | 0.1 | 0.13 | 0.11 | 0.10 | 0.093 |
| 14 | 0.870 | 0.758 | 0.661 | . 57 | 505 | 0.4 | 0.388 | 0.34 | 0.299 | 0.263 | 0.23 | 0.205 | 0.18 | 0.160 | 0.141 | 0.12 | 0.111 | 0.09 | 0.08 | 0.078 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0. | 0.362 | 0.315 | 0.275 | 0.239 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.07 | 0.065 |
| 16 | 0.853 | 0.728 | 0.623 | 0.534 | 0.458 | 0.39 | 0.339 | 0.292 | 0.252 | 0.218 | 0.188 | 0.163 | 0.141 | 0.123 | 0.107 | 0.093 | 0.081 | 0.071 | 0.062 | 0.054 |
| 17 | 0.844 | 0.714 | 0.605 | . 513 | 0.436 | 0.37 | 317 | 0.270 | 0.231 | 0.198 | 0.170 | 0.146 | 0.125 | 0.108 | 0.093 | 0.08 | 0.069 | 0.060 | 0.052 |  |
| 18 | 0.836 | 0.700 | 0.587 | 0.494 | 0.416 | 350 | 296 | 250 | 0.212 | 0.180 | 0.153 | 0.130 | 0.111 | 0.095 | 0.081 | 0.06 | 0.059 | 0.051 | 0.044 | 0.038 |
| 19 | 0.828 | 0.686 | . 51 | 0.475 | 0.396 | 0.331 | 0.277 | 0.232 | 0.194 | 0.164 | 0.138 | 0.116 | 0.098 | 0.083 | 0.070 | 0.06 | 0.051 | 0.043 | 0.037 | 0.03 |
| 20 | 0.820 | 0.673 | 0.554 | 0.456 | 0.377 | 0.312 | 0.258 | 0.215 | 0.178 | 0.149 | 0.124 | 0.104 | 0.087 | 0.073 | 0.061 | 0.051 | 0.043 | 0.037 | 0.031 | 0.026 |
| 25 | 0.780 | 0.610 | 0.478 | 0.375 | 0.295 | 0.233 | 0.184 | 0.146 | 0.116 | 0.092 | 0.074 | 0.059 | 0.047 | 0.038 | 0.030 | 0.024 | 0.020 | 0.016 | 0.01 |  |
| 30 | 0.742 | 0.552 | 0.412 | 0.308 | 0.231 | 0.174 | 0.131 | 0.099 | 0.075 | 0.057 | 0.044 | 0.033 | 0.026 | 0.020 | 0.015 | 0.012 | 0.009 | 0.007 | 0.005 | 0.004 |
| 35 | 0.7 | 0.5 | 0. | 0.2 | 0.181 | 0.1 | 0.094 | 0.068 | 0.049 | 0.036 | 0.026 | 0.019 | 0.014 | 0.010 | 0.008 | 0.006 | 0.004 | 0.003 | 0.002 | 0.002 |
| 40 | 0.672 | 0.453 | 0. | 0.2 | 0.142 | 0.097 | 0.067 | 0.046 | 0.032 | 0.022 | 0.015 | 0.011 | 0.008 | 0.005 | 0.004 | 0.003 | 0.002 | 0.001 | 0.001 | 0.00 |
| 50 | 0.608 | 0.372 | 0.228 | 0.141 | 0.087 | 0.0 | 0.034 | 0.021 | 0.013 | 0.009 | 0.005 | 0.003 | 0.002 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 |  |


| Future value interest factor of an ordinary annuity of \$1 per period at $\mathrm{i} \%$ for n periods, $\mathrm{FVIFA}(\mathrm{i}, \mathrm{n})=\$ 1^{*}\left(1+(1+\mathrm{i})+(1+\mathrm{i})^{\wedge} 2+. .(1+\mathrm{i})^{\wedge}(\mathrm{n}-1)\right.$ ) . |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Period | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |
|  | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 0 | , 00 | . 00 | . 000 | 1.000 | 1.000 | 1.000 | . 000 | . 000 |
| 2 | 2.010 | 020 | . 030 | . 040 | 050 | 60 | 70 | 80 | 90 | 00 | 110 | . 120 | 2.130 | 2.140 | 2.150 | . 160 | 2.170 | 2.180 | . 190 | 200 |
|  | 3.030 | 3.060 | . 091 | 3.122 | 153 | 184 | 3215 | 3.246 | 3.278 | 3.310 | 342 | . 374 | 3.407 | 3.440 | 3.473 | 506 | 3.539 | . 57 | 3.606 | 泷 |
|  | 4.060 | 4.122 | 4.184 | 4.246 | 4.310 | 4.375 | . 440 | 4.506 | 573 | 4.641 | 710 | 4.779 | 4.850 | 4.921 | 4.993 | 5.066 | 5.141 | 5.215 | 5. 291 | . 368 |
| 5 | 5.101 | 204 | 5.309 | 5.416 | 5.526 | 5.637 | 5.751 | 67 | 5.985 | . 10 | 6.228 | 6.353 | 6.480 | 6.6 | 6.742 | . 87 | 7.014 | 7.15 | 7.29 | . 442 |
| 6 | 6.152 | 6.308 | 6.468 | 633 | 802 | 975 | 153 | 33 | 523 | . 71 | 7.913 | . 115 | 8.323 | 8.536 | 8.754 | 8.977 | 9.207 | 9.442 | 9.683 | . 930 |
| 7 | 7.214 | 7.434 | 7.662 | 7.898 | 8.142 | 8.394 | 8.654 | 8.923 | 9.200 | 9.487 | 9.783 | 10.089 | 10.405 | 10.730 | 11.067 | 11.414 | 11.772 | 12.142 | 2.523 | 2.916 |
| 8 | 8.286 | 8.583 | 8.892 | 214 | 549 | 9.897 | 10.260 | 10.637 | 11.028 | 11.436 | 11.859 | 12.300 | 12.757 | 13.233 | 13.727 | 14.240 | 14.773 | 15.327 | 15.902 | 16.499 |
|  | 9.369 | 9.755 | 10.159 | 10.583 | 11.027 | 11.491 | 11.978 | 12.488 | 13.021 | 13.579 | 14.164 | 76 | 15.416 | 16.085 | 16.786 | 17.519 | 18.285 | 19.086 | 19.923 | 20.799 |
| 10 | 10.462 | 10.950 | 11.464 | 12.006 | 12.578 | 13.181 | 13.816 | 14.487 | 15.193 | 15.937 | 22 | 17. | 18. | 19. | 20.3 | 21.3 | 22. | 23.521 | 24. | 25. |
| 11 | 11.567 | 12.169 | 12.808 | 13.486 | 14.20 | 14.972 | 15 | 6.645 | 17.5 | 18.531 | 19.561 | 20.6 | 21.814 | 23.045 | 24.349 | 25.733 | 27.200 | 28.755 | 30.404 | 32.150 |
| 12 | 12.68 | 13 | 14.192 | 15.026 | 15 | 16.870 | 17.888 | 18 | 20.141 | 21.384 | 22.713 | 24.133 | 5.650 | 27.271 | 29.002 | 30.850 | 32.824 | 34.931 | 37.180 | 39.581 |
| 13 | 13 | 14. | 15.6 | 16 | 17 | 18.88 | 20.141 | 21.495 | 22.953 | 24.523 | 26.212 | 28.029 | 29.985 | 32.089 | 34.352 | 36.786 | 39.404 | 42.219 | 45.244 | 8.497 |
| 14 | 14.947 | 15.974 | 17.086 | 18.292 | 19.599 | 21.015 | 22.550 | 24.215 | 26.019 | 27.975 | 30.095 | 32.393 | 34.883 | 37.581 | 40.50 | 43.67 | 通 | 50.818 | 4.84 | . 196 |
| 15 | 16.097 | 17.293 | 18.599 | 20.024 | 21.579 | 23.276 | 25.129 | 27.152 | 29.361 | 31.77 | 34.405 | 37.280 | 40.417 | 43.842 | 47.580 | 51.66 | 110 | 65 | 66.261 | 2.035 |
| 16 | 17.258 | 18.639 | 20.157 | 21.825 | 23.65 | 25.673 | 7.888 | 30.32 | 33.003 | 35.950 | 39.190 | 42.7 | 46.672 | 50.980 | 55.71 | 60.925 | 66.649 | 72.939 | 9.8 | 87.442 |
| 17 | 18.4 | 20.01 | 21.7 | 23.6 | 25.8 | 28.213 | 30.840 | 33.7 | 36.974 | 40.545 | 44.501 | 48.884 | 53.739 | 59. | 65.0 | 1.6 | 8.9 | 87.0 | 96.0 | 105.93 |
| 18 | 19.6 | 21.4 | 23 | 25.6 | 28.1 | . 90 | 33.999 | 37.450 | 41.301 | 5.599 | 50.38 | 5.75 | 1.725 | 68.394 | 75.8 | 84.141 | 93.4 | 103.74 | 5.27 | 8.12 |
| 19 | 20.811 | 22.841 | 25.117 | 27.671 | 30.539 | 33.760 | 37.379 | 41.446 | 46.018 | 51.159 | 56.939 | 63.440 | 7.749 | 78.969 | 88.212 | 98.603 | 110.28 | 123.41 | 138.17 | 154.74 |
| 20 | 22.019 | 24.297 | 26.870 | 29.778 | 33.066 | 36.786 | 40.995 | 45.762 | 51.160 | 57.275 | 64.203 | 72.052 | 80.947 | 91.025 | 102.44 | 115.38 | 130.03 | 146.63 | 165.42 | 186.69 |
| 25 | 28.243 | 32.030 | 36.459 | 41.646 | 47.727 | 54.865 | 63.249 | 73.106 | 84.701 | 98.347 | 114.41 | 133.33 | 155.62 | 181.87 | 212.79 | 249.21 | 292.10 | 342.60 | 402.04 | 471.98 |
| 30 | 34.785 | 40.568 | 47.575 | 56.085 | 66.439 | 79.058 | 94.461 | 113.28 | 136.31 | 164.49 | 199.02 | 241.33 | 293.20 | 356.79 | 434.75 | 530.31 | 647.44 | 790.95 | 966.71 | 1,181.9 |
| 35 | 41.660 | 49.994 | 60.462 | 73.652 | 90.320 | 111.43 | 138.24 | 172.32 | 215.71 | 271.02 | 341.59 | 431.66 | 546.68 | 693.57 | 881.17 | 1,120.7 | 1,426.5 | 1,816.7 | 2,314.2 | 2,948.3 |
| 40 | 48.886 | 60.402 | 75.401 | 95.026 | 120.80 | 154.76 | 199.64 | 259.06 | 337.88 | 442.59 | 581.83 | 767.09 | 1,013.7 | 1,342.0 | 1,779.1 | 2,360.8 | 3,134.5 | 4,163.2 | 5,529.8 | 7,343.9 |
| 50 | 64.463 | 84.579 | 112.80 | 152.67 | 209.35 | 290.34 | 406.53 | 573. | 815.08 | 1,163 | 1, | 2,400.0 |  | , | , 717. | 10,436 | 15,090 | 21,813 | 31,515 | 45,497 |


| Present value interest factor of an (ordinary) annuity of \$1 per period at $\mathrm{i} \%$ for n periods, PVIFA $(\mathrm{i}, \mathrm{n})=\$ 1^{*}\left(1 /(1+\mathrm{i})+1 /(1+\mathrm{i})^{\wedge} 2+1 /(1+\mathrm{i})^{\wedge} 3 \ldots 1 /(1+\mathrm{i})^{\wedge} \mathrm{n}\right)$. |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Period | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 |
| 3 | 2.941 | 2.884 | 2.829 | 2.775 | 2.723 | 2.673 | 2.624 | 2.577 | 2.531 | 2.487 | 2.444 | 2.402 | 2.361 | 2.322 | 2.283 | 2.246 | 2.210 | 2.174 | 2.140 | 2.106 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | 3.387 | 3.312 | 3.240 | 3.170 | 3.102 | 3.037 | 2.974 | 2.914 | 2.855 | 2.798 | 2.743 | 2.690 | 2.639 | 2.589 |
| 5 | 4.853 | 4.713 | 4.580 | 4.452 | 4.329 | 4.212 | 4.100 | 3.993 | 3.890 | 3.791 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | 3.199 | 3.127 | 3.058 | 2.991 |
| 6 | 5.795 | 5.601 | 5.417 | 5.242 | 5.076 | 4.917 | 4.767 | 4.623 | 4.486 | 4.355 | 4.231 | 4.111 | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 |
| 7 | 6.728 | 6.472 | 6.230 | . 002 | 5.786 | 5.582 | 5.389 | 5.206 | . 033 | 4.868 | . 71 | 4.564 | 4.423 | 4.288 | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 |
| 8 | 7.652 | 7.325 | 7.020 | . 733 | 6.463 | 6.210 | 5.971 | 5.747 | 5.535 | 5.335 | 5.146 | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 |
| 9 | 8.56 | 8.16 | 7.786 | 7.435 | 7.108 | 6.802 | 6.515 | 6.247 | 5.995 | 5.759 | 5.537 | 5.328 | 5.132 | 4.946 | 4.772 | 4.607 | 4.451 | 4.303 | 4.163 | 4.031 |
| 10 | 9.471 | 8.983 | 8.530 | 8.111 | 7.722 | 7.360 | 7.024 | 6.710 | 6.418 | 6.145 | 5.889 | 5.650 | 5.426 | 5.216 | 5.019 | 4.833 | 4.659 | 4.494 | 4.339 | 4.192 |
| 11 | 10.368 | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | 7.139 | 6.805 | 6.495 | 6.207 | 5.938 | 5.687 | 5.453 | 5.234 | 5.029 | 4.836 | 4.656 | 4.486 | 4.327 |
| 12 | 11.255 | 10.575 | 9.954 | 9.385 | 8.863 | 8.384 | 7.943 | 7.536 | 7.161 | 6.814 | 6.492 | 6.194 | 5.918 | 5.660 | 5.421 | 5.197 | 4.988 | 4.793 | 4.611 | 4.439 |
| 13 | 12.134 | 11.348 | 10.635 | 9.986 | 394 | 853 | 8.358 | 7.904 | 7.487 | 7.103 | 6.750 | 6.424 | 6.122 | 5.8 | 5.58 | 5.3 | 5.11 | 4.910 | 4.715 | 4.533 |
| 14 | 13.004 | 12.106 | 11.296 | 10.563 | 9.899 | 9.295 | 8.745 | 8.244 | 7.786 | 7.367 | 6.982 | 6.628 | 6.302 | 6.002 | 5.724 | 5.468 | 5.229 | 5.008 | 4.802 | 4.611 |
| 15 | 13.865 | 12.849 | 11.938 | 11.118 | 10.380 | 9.712 | 9.108 | 8.559 | 8.061 | 7.606 | 7.191 | 6.811 | 6.462 | 6.142 | 5.847 | 5.575 | 5.324 | 5.092 | 4.876 | 4.675 |
| 16 | 14.718 | 13.578 | 12.561 | 11.652 | 10.838 | 10.106 | 9.447 | 8.851 | 8.313 | 7.824 | 7.379 | 6.974 | 6.604 | 6.265 | 5.954 | 5.668 | 5.405 | 5.162 | 4.938 | 4.730 |
| 17 | 15.562 | 14.292 | 13.166 | 12.166 | 11.274 | 10.477 | 9.763 | 9.122 | 8.544 | 8.022 | 7.549 | 7.120 | 6.729 | 6.373 | 6.047 | 5.749 | 5.475 | 5.222 | 4.990 | 4.775 |
| 18 | 16.398 | 14.992 | 13.754 | 12.659 | 11.690 | 10.828 | 10.059 | 9.372 | 8.756 | 8.201 | 7.702 | 7.250 | 6.840 | 6.467 | 6.128 | 5.818 | 5.534 | 5.273 | 5.033 | 4.812 |
| 19 | 17.226 | 15.678 | 14.324 | 13.134 | 12.085 | 11.158 | 10.336 | 9.604 | 8.950 | 8.365 | 7.839 | 7.366 | 6.938 | 6.550 | 6.198 | 5.877 | 5.584 | 5.316 | 5.070 | 4.843 |
| 20 | 18.046 | 16.351 | 14.877 | 13.590 | 12.462 | 11.470 | 10.594 | 9.818 | 9.129 | 8.514 | 7.963 | 7.469 | 7.025 | 6.623 | 6.259 | 5.929 | 5.628 | 5.353 | 5.101 | 4.870 |
| 25 | 22.023 | 19.523 | 17.413 | 15.622 | 14.094 | 12.783 | 11.654 | 10.675 | 9.823 | 9.077 | 8.422 | 7.843 | 7.330 | 6.873 | 6.464 | 6.097 | 5.766 | 5.467 | 5.195 | 4.948 |
| 30 | 25.808 | 22.396 | 19.600 | 17.292 | 15.372 | 13.765 | 12.409 | 11.258 | 10.274 | 9.427 | 8.694 | 8.055 | 7.496 | 7.003 | 6.566 | 6.177 | 5.829 | 5.517 | 5.235 | 4.979 |
| 35 | 29.409 | 24.999 | 21.487 | 18.665 | 16.374 | 14.498 | 12.948 | 11.655 | 10.567 | 9.644 | 8.855 | 8.176 | 7.586 | 7.070 | 6.617 | 6.215 | 5.858 | 5.539 | 5.251 | 4.992 |
| 40 | 32.835 | 27.355 | 23.115 | 19.793 | 17.159 | 15.046 | 13.332 | 11.925 | 10.757 | 9.779 | 8.951 | 8.244 | 7.634 | 7.105 | 6.642 | 6.233 | 5.871 | 5.548 | 5.258 | 4.997 |
| 50 | 39.196 | 31.424 | 25.730 | 21.482 | 18.256 | 15.762 | 13.801 | 12.233 | 10.962 | 9.915 | 9.042 | 8.304 | 7.675 | 7.133 | 6.661 | 6.246 | 5.880 | 5.554 | 5.262 | 4.999 |

